# Year 6 Maths Knowledge Organisers Spring

Week	Week	Week	Week	Week	Week	Week	Ŧ	Week	Week	Week	Week	Week
1	2	3	4	5	6	7		1	2	3	4	5
4OPs Place value  + & -  X & ÷		erimeter olume	<u>Statistics</u>	<u>Algebra</u>	Conversion/time	Shape  1 Shape 2	Half term	Ratio and proportion	<ul> <li>Place</li> <li>+ &amp; -</li> <li>X &amp; ÷</li> </ul>	value •	Algebra Shape 1 Shape 2 Convers Statistic	ion/time

Click on a maths area

- 1 more
- 1 less
- Greater than
- Less than
- Equal
- Equivalent
- Millions
- **Thousands**
- Hundreds
- **Tens**
- Ones
- Zero
- Place Value
- Order
- Round
- Negative Number
- Digit

#### More or Less +1,000 Number 1,000 more 4,600 5,600 6,643 7,643 9,021 8,021

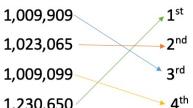
# 1,230,650

**Place Value** 

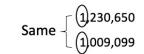
Y5/6

#### **Ordering**

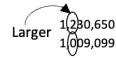
Order from largest to smallest



· Look at the largest digit first (millions)



• Then go to the next digit. If the digit it greater, then the number is larger



#### Rounding

Round 3,576,219 to the nearest million

Identify the millions

(3)576,219

Look at the digit beside the millions

Rounding rhyme – 0,1,2,3,4 stays the number before

-1,000

5,6,7,8,9 rounds up on the number line

So, rounding 3,576,219 to the nearest million will mean it will round up on the number line because of the 5 digit in the hundred thousands.

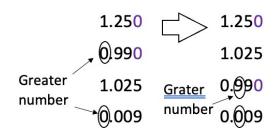
4,000,000

#### **Ordering Decimals**

Order starting with the smallest

1.25 0.99 1.025 0.009

Add place holders (write zeros) and follow the steps above



#### **Roman Numerals**

**| = 1** · Bridging numbers Value = 5 V,L and D (you can't have 2 together)

Xylophones = 10 ● Top rule - you cannot have more than 3 of the same letter in a row

Like = 50

**MMXXIII** = 2023

Cows = 100 Do = 500

Milk = 1000

#### Recognise value of digits

What is the value of 4?

1,042,851

Move from the ones across writing the value of the column above



Forty thousand



- ➤ Add
- Plus
- > Total
- > Sum
- Altogether
- > Equals
- Digit
- Tens
- Ones
- Hundreds
- Subtract
- Minus
- > Take away
- Regroup

#### Add and subtract mentally

1.3 digit and ones

Circle the ones and subtract

2.3-digits and tens Circle the tens and add 839 + 60 = 899

$$3 + 6 = 9$$

3. 3-digit and hundreds
Circle the hundreds
649 – 400 = 249

$$6 - 4 = 2$$

Prove all with resources and drawings in school. E.g.

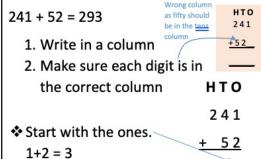
$$243 - 30 = 213$$



## Column addition example

	4	5	8	6	4
+	2	3	4	9	7
	6	9	3	6	1
		1	1	1	

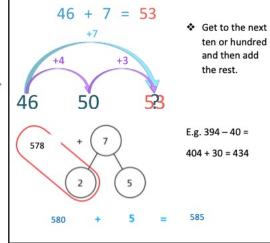
#### **Column addition (without regrouping)**



Then go to the tens.

2,93

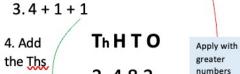
#### Mental addition and subtraction bridging



## Addition and subtraction Y5/6

#### Column addition (with regrouping)

1. Start with ones, 2 + 8 = 10
So regroup by carrying
The 1 to the tens column



2 482 number up to 1
+ 3 138
5 620

#### Column subtraction example

	3	5	<sup>6</sup> 7	13 <b>/</b> 4	<sup>1</sup> ⁄2′
_		3	4	7	6
	3	2	2	6	6

## <u>Column subtraction (with regrouping)</u>

- ➤ Start with ones, 5 7, you cannot do so regroup by taking one ten from the 7, leaving 6 tens, and put in the ones column to make 15. 15 6 = 9
- ➤ Next, the tens. 6 8, you cannot do so regroup by taking one of the hundreds, leaving 7 hundred, and put it in the tens column to make 16.

$$16 - 8 = 8$$

$$\triangleright$$
 Finally,  $7-2=5$ 



589

You cannot do 5 – 7 so go to the tens column. Take a ten to leave 6 tens and make 15 in the ones column.



Click here to

- **≻**Multiply
- ➤ Multiplication
- ➤ Lots of
- **≻**Times
- **▶** Division
- ▶ Grouping
- **>** Sharing
- **≻**Arravs

#### **Short division**

 $217 \div 7 = 31$ 

- 1. This division is quicker because you are dividing by a times table up to 12. This example is dividing by 7.
- 2. Write in a bus stop

7 217

3. Look at the first digit in 217. How many 7s are in 2? Zero.

	U	-	_
7	(2	1	7

4. Look at the next digit with the 2. How many 7s in 21? Three.

	031	į
7	21)7	

5. How many 7s in 7? One.

#### Highest common factor (HCF)

What is a factor?

- A factor is a number that goes into another number.
- . LCF is when you compare 2 or more numbers, list their factors and identify what factor is common between them. The highest value is the HCF.

Top tip - list the factors as pairs and start from 1, then go to 2, 3, etc. ctors for 12

	Fa	
actors		
1	16	1
2	8	2
	٥	3
4	4	
		- [

HT0

324

<u>3 2</u>4

X 1 3

9 7 2 HTO

3 2 4

X 13

972

3 2 4 0

4212

What is the HCF for 16 and 12?

4 is the HCF.

Multiplication and

division Y5/6

2 is a common factor but it isn't the highest.

#### 0 - orders (squared or cubed)

Order of operations

Remember BODMAS

D - division

B - brackets

M - multiplication

A – addition

S - subtraction

Follow this order to complete calculations correctly.

E.g.  $(16-10) \div 3 = ?$ 

1. Brackets 1st, so 16-10=6

2. Then,  $6 \div 3 = 2$ 

So, (16-10) ÷ 3

equals 2.

**Important facts** 

#### **Apply times tables**

you know...  $2 \times 8 = 16$ 20 has a 0 so your 20 x 8 = 160 1

If you know  $2 \times 8 = 16$ , then

will have 1 zero as  $2 \times 80 = 160$ it is 10x

Top tip – look at the number of zeros. This tells you if you need to write any zeros in your answern total, 20 and

20 x 80 = 1600

zeros as it is 100x greater

#### Column multiplication

324 x 13

1. Write the calculation in a column. Make sure the digits are in the correct column. HT0







- 2. Start with multiplying the 3 in 13 with the ones column. So,
- 3x4 =12. Carry the 1 in the number 12 into the tens column. 3. Move onto 3x2 (the tens column) and add the extra 1 that you H T O carried, 3x2=6, add 1=7
- 4. Then, 3x3 (in the hundreds column), which is 9
- 5. You have multiplied the 3 in 13, now move onto the 1 ten in 13.
- 6. Put a zero (0) in the ones column as we are x by 10 not 1.
- 7. Then follow the same process described in the previous Steps but multiplying each digit by 1 instead (1x4,1x2,1x3)
- 8. Finally, 972 + 3240 = 4212. Use the column method (see the addition and subtraction KO for support)

#### Long division

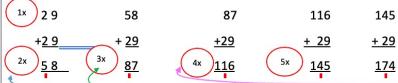
$$6786 \div 29 = 234$$

29 6786

#### Anything x0 is always 0 as you do not have

any groups.

1. You don't know the 29x table? Calculate the first 5 numbers in the 29x table by adding 29 five times.



2. 29 6786

How many 29s in 6? Zero. So go to the next digit to make 67 and write 0.

023 4. 29 6 786

How many in 98? Three. 98-87=11

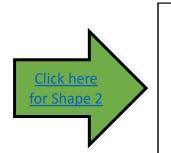
02 3. 29 6 7 8 6

How many 29s in 67? Use your notes to help. Two times. 67-58=9. Carry the 9 to the next column. 0234

5. 29 6 7 8 6

How many 29s in 116? Four times.





- **≻**Angle
- ➤ Right Angle
- ➤ Acute Angle
- ➤ Obtuse Angel
- ➤ Reflex Angle
- ➤ Triangle
- ➤ Isosceles Triangle
- ➤ Scalene Triangle
- ➤ Right Angled Triangle
- **≻**Equilateral Triangle
- **➢** Diameter
- ➤ Vertically opposite
- **≻**Angles

# **The Angles** Right Angles are 90° 90° but less than 180°

Vertically opposite angles are

always the same

 $35^{\circ}$ 

other side is 35°

180° to find b.

 $180^{\circ} - 35^{\circ} = 145^{\circ}$ 

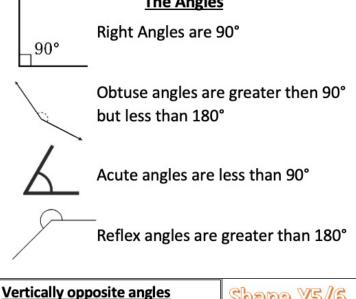
so have a total of 180°

1. If one side is 35° then the

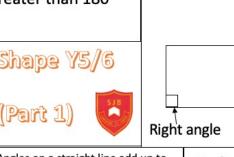
altogether. Subtract 35 from

e.g.

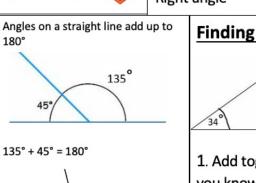
# Obtuse angles are greater then 90° Acute angles are less than 90° Reflex angles are greater than 180°

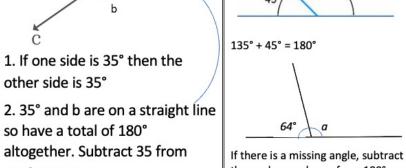






**〈**60°





#### the angles you know from 180° 180° - 64° = 116° a=116°

## Finding missing angles

Angles in a triangle

add up to 180°

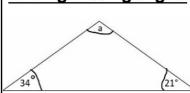
Labelling a 2D shape

Side

60° x 3

= 180°

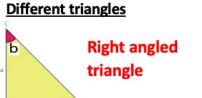
Corner



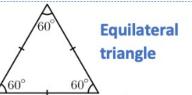
1. Add together the angles you know

2. Subtract this total from 180

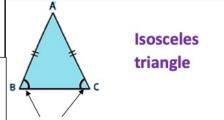
 $a = 125^{\circ}$ 



- 1. It has an angle measuring 90°, which is shown by the square
- 2. The other 2 angles add up to 90°  $(a + b = 90^{\circ})$



- 1. All angles are 60°
- 2. All sides are the same



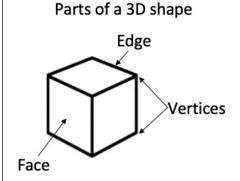
- 1. Two angles are equal
- 2. Two lengths are equal



- .1. All angles are different
- .2. All lengths are different
- \* Remember all angles in a triangle add up to 180°!



- ≥3D shapes
- **≻**Cube
- **≻**Cuboid
- **≻**Sphere
- ➤ Square based pyramid
- **≻**Tetrahedron
- ➤ Triangular prism
- ➤ Vertices
- **≻**Edges
- **≻** Faces
- ➤ Angles
- ➤ Degrees
- **≻**Radius
- ➤ Diameter
- **≻**Volume



Radius and diameter

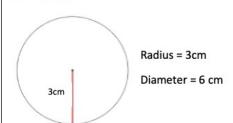


Diameter is the distance from one side of the circle to the opposite side of the circle.



Radius is the distance from the middle of the circle to the side.

The diameter is twice as long as the radius



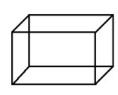


Cube

Faces = 6

Vertices = 8





Cuboid

Faces = 6

Vertices = 8

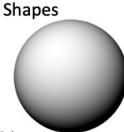
Edges = 12

Tetrahedron

Vertices = 4

Faces = 4

Edges = 6



Sphere

Faces = 1

Vertices = 0

Edges = 0



Triangular prism

Square based pyramid

Faces = 5

Edges = 8

Vertices = 5

Faces = 5

Vertices = 6

Edges = 9

Shape

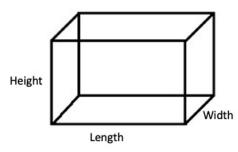
Y6 (Part 2)

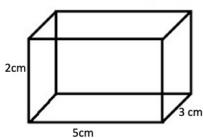
#### Volume

Volume is the 3D space something can hold

Volume = length x width x height

The units in volume always end in <sup>3</sup> for cubed (<u>e.g.</u> cm<sup>3</sup>)





 $5 \times 3 \times 3 = 12 \text{cm}^3$  $6 \times 2 = 12 \text{cm}^3$ 





Click here to return to

> selection page

#### Vocabulary

- > Fraction
- ➤ Part
- > Whole
- ➤ Equal
- > Share
- ➤ Half
- ➤ Quarter
- **➤** Third
- ➤ Equivalent
- **➤** Numerator
- ➤ Denominator
- ➤ Proper Fraction
- > Improper Fraction
- > Factor
- ➤ Highest Common Factor
- ➤ Lowest Common Multiple
- ➤ Simplify
- ➤ Simplest Form
- ➤ Mixed Number
- ➤ Whole Number

#### **Subtract fractions**

Lowest common multiple

8=8,16,24,32,40

5=5,10,15,20,25,30,35,<mark>40</mark>

$$\frac{7}{8} - \frac{3}{5}$$

$$x5\left(\frac{35}{40} - \frac{24}{40}\right) x8 = \frac{11}{40}$$

#### **Add Fractions**

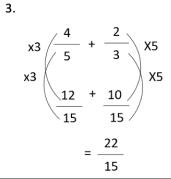
1. Find a common multiple of 5 and 3

$$\begin{array}{c}
\underline{e.g.} \, 15 \\
4 \\
5 \\
+ \\
\hline
15
\end{array}$$

$$\begin{array}{c}
\times 3 \\
\times 5 \\
+ \\
\hline
15
\end{array}$$

$$\begin{array}{c}
\times 5 \\
\times$$

Whatever you do to the top you must do to the bottom



#### **Divide fractions**

4		2		
7	<del>-</del>	5		
Stay C	hange	Flip		
4		5		20
	X	2	=	14
7		2		6
			=	1—
				14
			=	1-3
				7

#### **Multiply Fractions**

$$\frac{5}{8}$$
 X  $\frac{3}{5}$ 

Times the top AND times the bottom

$$\frac{5 \times 3}{8 \times 5}$$

$$= \frac{15}{40}$$

#### Fractions



Mixed number →Improper Fractions

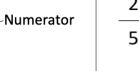
2 
$$\frac{3}{5}$$
 1. Multiply whole number by the denominator

- $2 \times 5 = 10$ 
  - 2. Add the number to the answer

Lowest common multiples

$$\frac{3}{8} + \frac{5}{12}$$

$$x3 \left( \frac{9}{24} + \frac{10}{24} \right) x2$$



Denominator

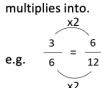
Divide by the bottom Times by the top

Of 15

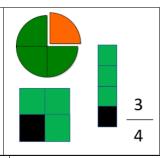
$$3 \times 2 = 6$$

$$\frac{2}{5}$$
 Of 15 = 6

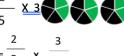
Common denominator = find another number that the bottom number (denominator)







Multiply fraction by Improper fractions ---mixed fractions



$$= \frac{2}{5} \times \frac{3}{1}$$

whole number





1. How many 3s in 17?

Subtract 15 from 17

Divide fraction by whole number

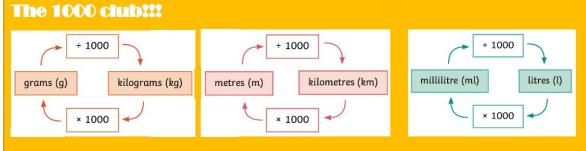
$$\frac{5}{7} \div 3$$

Turn whole number into fraction so  $3 = \frac{1}{2}$ Stay Change Flip

$$\frac{5}{7}$$
 X  $\frac{1}{3} = \frac{3}{21}$ 

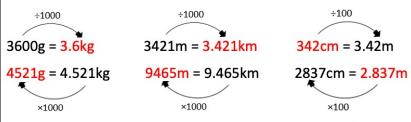
- Measure
- Compare
- Add
- Subtract
- Mass
- Volume
- Millilitres (ml)
- Litres (I)
- Kilograms (kg)
- Grams (g)
- Metres (m)
- Centimetres (cm)
- Millimetres (mm)
- Perimeter
- Time
- Analogue
- Digital
- Hours
- Minutes
- Seconds
- O'clock
- Half past
- Quarter past/to
- Midday
- Am and pm

#### Conversion

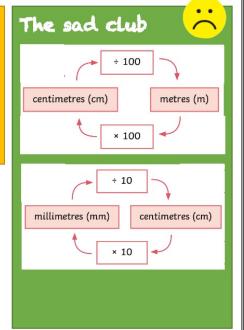


#### Kilo = 1000

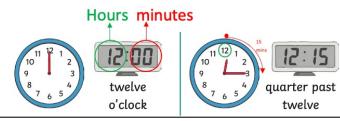
Children learn what the 1000 club is which means you always multiply or divide by 1000.

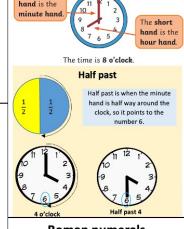


# Conversion and time Y5/6

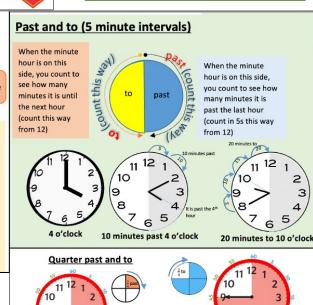


#### **Digital and analogue**





Telling the time - o'clock



quarter past

quarter to

#### How we measure time?

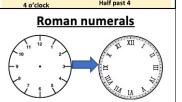












- **≻**Algebra
- **≻**Sequences
- > Expressions
- **≻**Equations
- **≻** Formulae
- **>** Unknowns
- ➤ Bar models

Multi-step problem (SATs Q)

Total value is 147
What is the value of each shape?

1. Label the shapes letters

a b b b

147

She gives each shape a value.

#### What is algebra?

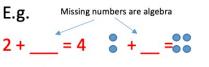
Believe it or not, algebra is used as early as Reception in school.

Algebra is when something other than a number is used in maths to represent a value (an unknown).

> Being confident with bar models will immensely

support a child's reasoning

in these questions.





12				
?	?	?	?*	

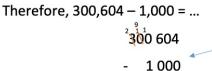
Question marks are also algebra as they are used instead of numbers and are unknown.

#### Algebra as number sequences

303,604 302,604 301,604 300,604

The symbol '...' is the unknown in this question. In order to find the unknown, you need to find the difference between the numbers in the sequence. Try it with two numbers.





299 604

See addition and subtraction knowledge organiser for column subtraction

#### Algebra

#### Y5/6

#### Algebra as bar models

4c					
С	С	С	С		
4d + 10					
d	d d	d 10	)		
t – 15 = 85					
		t			

ab = 18			
а	b		

2

18

_			
	b	а	b
	18	2	6
	9	3	4
	6	4	2
	3	5	0
	2	Children sh	a ulal
	1	Children sh explore dif	

2a + b = 10

combinations in these

questions.

Equations with a

pair of unknowns

In an equation with two unknown

numbers, there may be several possible values for the unknowns that will

balance the equation.

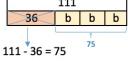
	-
t	
85	15

#### 3. The only difference between the first and second shape is the first

shape has one more 'a', so 147-111= a as subtracting finds the difference. So, a=36 147

111

#### 4. If we know a=36, then...



#### 5. Finally, $75 \div 3 = 25$

75	1
b	b
	b

#### Expressions are a group of numbers and letters without the equals (=) sign. E.g. a + 10 or b - c

Algebra notation

Any letter or symbol can be used to

represent a number.

Adding

a + 14 means you are adding 14 to a.

(e.g. if a=12, then 12+14=26)

Subtracting

a - 10 means you are subtracting 10

from a.

(e.g. if a=20, then 20-10=10)

Multiplying

4a means 4 times the value of a (e.g. if

a=2, then 4x2=8)

**Dividing** 

a ÷ 5 means how many 5s are in the

value of a?

(e.g. if a=15, then 15÷5=3)

More than one operation

You must use BODMAS (see addition

and subtraction knowledge organiser).

4a - 10 means multiply a by 4 and then subtract 10 from this number.

(e.g. if a=4, then 4x4=16, then subtract

10 = 6)

Equations are a group of numbers and letters with an equals (=) sign. E.g. a + 10 = 12 or b - c = 1

Formulae show how to calculate something, such as the area of a square (area = base x width)





2. So the first shape is 2a + 3b = 147 and the second is a + 3b = 111

Total value is 111

Replace the letter 111 a with 36 b b

111





### <u>Vocabulary</u>

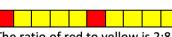
- ➤ Ratio
- **≻**Proportion
- ➤ Bar model
- **≻**Multiply
- **≻**Multiplication
- **≻**Lots of
- **≻**Times
- **➢** Division
- ➤ Grouping
- **>** Sharing
- **≻**Arrays

**SATs Q** 

#### What is ratio?

Ratio compares the amounts of two or more things.

Example 1



The ratio of red to yellow is 2:8 as there are 2 red and 8 yellow.

Example 2



The ratio of blue to green to orange is 2:5:3.

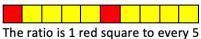


#### Proportion uses the ratio to f

What is proportion?

Proportion uses the ratio to find different amounts of a total and/or simplifies a ratio.

E.g.



The ratio is 1 red square to every ! yellow squares.

The ratio is 1:4

The original ratio was 2:8 (there are 2 red squares and 8 yellow squares).



2:8 = 1:4

#### Ratio &



Y5/6

#### Ratio and proportion word problems (abstract)

- ➤ Jill has a bag of 16 sweets. She has 1 orange sweet for every 3 red sweets.
- 1. What is the ratio of orange to red sweets? 1:3

There are 4 orange sweets and 12 green sweets  $(4 \times 3 = 12)$ .

Ratio and proportion word problems (using the bar model)

a. What is the ratio of orange to red sweets? 1:3

b. How many orange sweets are there?

Draw a bar model for each part of the ratio.

5. Jill has a bag of 16 sweets. She has 1 orange sweet for every 3 red

16 sweets in total.

There are 4 parts.

So, 4 goes into each box

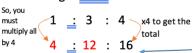
 $16 \div 4 = 4$ 

- 2. How many orange sweets are there?
- 3. Write the ratio along with the total of the ratio (4 here)

Orange: Red: Total

sweets.

Orange



4. 1 x 4 = 4, so there are 4 orange sweets.

 $3 \times 4 = 12$ , so there are 12 red sweets

Stefan wants to make some of this green paint.

He uses 750 ml of blue paint.

• 250 ml of blue paint

• 1,150 ml of yellow paint.

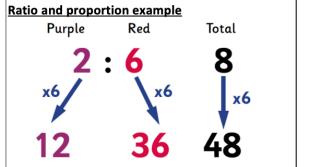
#### How much green paint does he make?

You can make green paint by mixing:

Blue : yellow : green (total)

 $^{250} = ^{1150} : 1400$ 

Answer: He made 4200ml of green paint.



Write the total number

underneath



#### Mean example

1.0	4.5
12	15
10	8
4.5	

15

12 + 15 + 10 + 8 + 15 = 60

60 ÷ 5 = 12

The mean of this data is 12.

#### Vocabulary

- Bar chart
- Pictogram
- Frequency table
- > Tally chart
- Pie chart
- Discrete data
- Continuous data
- ➤ Line graph
- > Sum
- Difference
- Comparison
- > Interpret
- Mean
- Average

#### Statistics Y5/6



#### **Tables and tally charts**

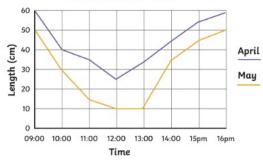
Method of Travel	Tally	Frequency
Walk	JHT 1111	9
Bike	III	3
Car	JHT I	6
Bus	11111/1111	12
	TOTAL	30

#### Line graph

Line graphs are used to show changes to a measurement over time.

It is used for continuous data (numbers that are not fixed).

#### A line graph to show the length of shadows over time

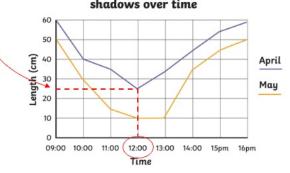


To find values on a line graph, your child must use a ruler to draw lines to find the corresponding value.

For example, what time was the length of the

shadow 25cm during April?

#### A line graph to show the length of shadows over time



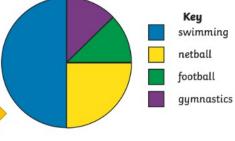
Mean is when you add up all the values and divide it by the total number of values.

#### Pie charts

Children should use what they know from previous years.







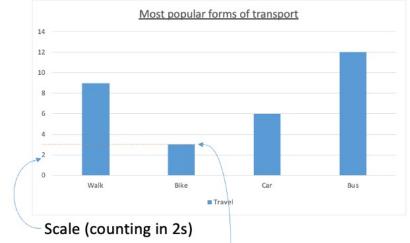
A pie chart to show children's

favourite sports

Use these fractions and the total to find out different values

24 children were asked in total. Swimming =  $\frac{1}{2}$  so  $\frac{1}{2}$  of 24 = 12 children Netball =  $\frac{1}{4}$  so  $\frac{1}{4}$  of 24 = 6 children Football =  $\frac{1}{8}$  so  $\frac{1}{8}$  of 24 = 3 children Gymnastics =  $\frac{1}{8}$  so  $\frac{1}{8}$  of 24 = 3 children

#### Bar chart



- To interpret a bar chart, children must draw a line to check the value of a bar.
- To draw a bar chart, the children must decide on a suitable scale, make sure the bars are an equal distance apart and the same thickness.



#### Vocabulary Area of rectangles **>** Perimeter length × width = area of a rectangle ➤ Area ➤ Volume 4cm **>** Units ➤ Width ➤ Length Counting squares: ➤ Rectangle 8cm > Formula $area = 18cm^2$ ➤ Height Use formula: **≻** Base 6cm × 3cm ➤ Parallelogram $area = 18cm^2$ $8cm \times 4cm area = 32cm^2$ Missing lengths Area, perimeter and Use 2 colours to show vertical and volume Y5/6 horizontal lines. +6=9 and 7+ == 15 Volume of cuboids length × width × height = volume of a cuboid height 3cm length 6cmwidth 4cm

# Multiply dimensions in any order: 3cm × 6cm × 4cm volume = 72cm<sup>3</sup>

Click here to

return to

selection

page

